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# Structure-Property Correlations in Cuprate Superconductors

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Received October 5, 1990 (Revised Manuscript Received March 11, 1991)

Superconductors are materials that permit electric currents to flow with no loss of energy. Also, they can act as perfect diamagnets in a magnetic field. These two unique features make superconductors technologically important in applications such as supercomputers, SQUIDS (superconducting quantum interference devices), Maglev (magnetic levitation) transportation, power storage and delivery, and communications, to name a few.<sup>Ia</sup> Due to their potential role in such applications, high-temperature cuprate superconductors have been extensively studied over the past several years.<sup>1b-d</sup> In understanding how these superconductors work, it is essential to know what structural and electronic factors determine the magnitude of their superconducting critical temperatures T<sub>c</sub>. Cuprate superconductors are layered metal oxides in which perovskite-type  $CuO_2$  layers are intergrown mostly with rock-salt-type MO (e.g., M = La, Sr, Ba, Bi, Tl) layers. The complexity of the cuprate structures has made it difficult to single out relevant physical parameters governing their superconductivity. Thus, the  $T_{\rm c}$  values of p-type cuprates have been correlated with a large

number of structural and electronic parameters, which include the hole density  $(n_{\rm H})$  in the CuO<sub>2</sub> layer,<sup>2</sup> the in-plane Cu-O bond lengths,<sup>3</sup> their bond valence sums,<sup>2a,4</sup> the hole density to effective mass ratios,<sup>5</sup> the Madelung potentials,<sup>6</sup> and the electronic density of states at the Fermi level.<sup>7</sup> General aspects of cuprate structures and bonding have been discussed in recent review articles.<sup>1b-d</sup> In this Account, we review several important structure-property correlations in the cuprate superconductors.

#### **Structural Characteristics**

Most p-type cuprate superconductors may be viewed as intergrowths of perovskite and rock-salt blocks. The rock-salt block is composed of AO (e.g., A = Bi, Tl) layers, and the perovskite block of  $CuO_2$  and M (e.g., M = Ca, Y layers, as shown in Figure 1. The "intergrown" region in common is the BO (e.g., La, Sr, Ba) layer, being structurally related to both the rocksalt and perovskite blocks. The  $CuO_2$  layers are built from corner-sharing square-planar  $\overline{CuO_4}$  units, and copper can be bonded to another oxygen atom, creating a square-pyramidal environment, or to two additional

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Figure 1. Schematic diagram showing the arrangement of atoms around a 9-coordinate site in p-type cuprate superconductors. The cations are represented by shaded circles.

oxygen atoms, giving an axially elongated octahedral surrounding. Compositionally, these superconductors have the formula  $(AO)_m(BO)_2(M)_{n-1}(CuO_2)_n$  and are often referred to as m2(n-1)n phases. The number of  $CuO_2$  layers that are stacked consecutively is as high as 5. When n = 1, only distorted CuO<sub>6</sub> octahedra are present. With n = 2, all of the Cu atoms are square pyramidal. For n > 3, the copper atoms of the outer two  $CuO_2$  layers are square pyramidal, and those of the inner ones are square planar. M is typically Ca, Y, or rare earths and is situated between adjacent CuO<sub>2</sub> sheets. A BO layer, with B = La, Sr, or Ba, is located directly above and below the  $(CuO_2)_n$  layers. Up to two AO layers can be stacked together: m = 2 for A = Bi, m = 1 or 2 for A = Tl, and m = 0 for B = La (e.g., La<sub>2</sub>CuO<sub>4</sub>). The superconductors  $YBa_2Cu_3O_7$  and  $YBa_2Cu_4O_8^{1d}$  are special cases of the m2(n-1)n series: The AO layer is replaced by a layer composed of CuO strings for m = 1 and CuO double strings for m = 2 [i.e.,  $(CuO)_m(BaO)_2(Y)_1(CuO_2)_2$ ]. Structural oxidation-reduction chemistry (e.g., cation substitution of  $Sr^{2+}$  for  $La^{3+}$  or  $Y^{3+}$  for  $Ca^{2+}$ ) in the AO, BO, and M layers leads to electron removal from (i.e., hole-doping) or electron addition to (i.e., electron-doping) the  $CuO_2$  layers.

## Interrelation between the Rock-Salt-Layer and **Perovskite-Layer** Distortions

In the p-type cuprate superconductors, the  $CuO_2$ sheets form a rigid, two-dimensional network with short Cu-O bonds. In an ideal square-planar perovskite layer, the in-plane Cu-O distance would be one-half the perovskite a axis, i.e.,  $\approx 1.9$  Å. This imposes the restriction that, if the atoms of the AO and BO layers are coplanar, the A-O and B-O intralayer distances be close to  $\approx 1.9 \times 2^{1/2} \approx 2.7$  Å for the ideal structures.<sup>8</sup> According to the ionic radii<sup>9</sup> for the 9-coordinate B cations (i.e., La<sup>3+</sup>, Sr<sup>2+</sup>, Ba<sup>2+</sup>), the 6-coordinate A cations (i.e.,  $Tl^{3+}$ ,  $Bi^{3+}$ ), and the 6-coordinate  $O^{2-}$  anion, the ideal A-O and B-O distances are estimated as Ba-O = 2.87Å, Sr-O = 2.71 Å, La-O = 2.62 Å, Bi-O = 2.43 Å, and Tl-O = 2.29 Å. Consequently, the perovskite-layer/ rock-salt-layer mismatch is severe for the BiO and TlO layers. The B atoms of a BO layer (B = Ba, Sr, La) lie below its oxygen atom plane toward the adjacent  $CuO_2$ layer, so that the CuO<sub>2</sub>-layer/BO-layer mismatch is severe for the LaO layer. To relieve these interlayer strains, the Bi, Tl, or La atoms are displaced from their ideal rock-salt sites to form shorter and stronger bonds

with oxygen.<sup>10</sup> The ideal rock-salt arrangement, viewed perpendicularly to one layer, is shown in 1a. More stable atomic configurations result when the metal and oxygen atoms are shifted to form ladder-like (1b), chain-like (1c), or island-like (1d) patterns in the Tl-O. Bi-O. or La-O lavers.



In all cuprates in which the rock-salt metal atom is connected to a copper atom by an O<sub>ax</sub> atom (see Figure 1), the Tl-, Bi-, or La- $O_{ax}$  bond is considerably shorter than the in-plane Tl-, Bi-, or La-O bonds (e.g., Bi- $O_{ax}$  $\approx 2.03$  Å versus in-plane Bi–O  $\approx 2.25$  Å). On the other hand, the Cu-O<sub>ax</sub> distance, 2.5–2.7 Å, is significantly longer than the in-plane Cu–O distances of  $\approx 1.9$  Å. Therefore, when the rock-salt atoms "move" within their layer, they also shift the O<sub>ax</sub> atom and cause the  $CuO_5$  square pyramids or  $CuO_6$  octahedra to tilt and consequently make the  $CuO_2$  sheets "buckle". A planar  $CuO_2$  sheet, shown in **2a**, can buckle in two ways, depending on how the rock-salt layer distorts. Ladder-



and chain-like distortions, 1b and 1c, give rise to a buckling, 2b, in which the copper square pyramids or octahedra form rows that alternately tip toward and away from each other. An island-like distortion, 1d. causes pairs of adjacent corner-shared copper polyhedra to tilt toward one another as shown in 2c.  $La_{2-x}Ba_xCuO_4$  ( $x \approx 0.1$ ) undergoes two phase transitions as a function of temperature:<sup>11</sup> It has a high-temperature tetragonal structure (HTT) that first transforms to a low-temperature orthorhombic phase (LTO) and then to a low-temperature tetragonal structure (LTT). The HTT, LTO, and LTT phases have the  $CuO_2$  structures 2a, 2b, and 2c, respectively. Rocksalt-layer distortions involve bond-length changes,

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which are energetically much stronger than CuO<sub>2</sub>-laver tilt distortions involving only bond-angle changes. Therefore, the CuO<sub>2</sub>-layer tilt occurs to satisfy the bonding requirements of the rock-salt La, Bi, or Tl atoms.

Effects of the rock-salt-layer/CuO<sub>2</sub>-layer mismatch are also manifested in other structural observations. For example, the orthorhombic structures of  $La_2CuO_4^{12}$ (with space group Bmab),  $Bi_2Sr_2CuO_6$ ,<sup>13</sup> and  $Bi_2Sr_3-_xCa_xCu_2O_8^{14}$  show the CuO<sub>2</sub>-layer structure of **2b**, which is buckled along the *b*-axis direction. Rigid  $CuO_2$ -layer buckling would make the *b*-axis length shorter than the a-axis length. However, the La–O or Bi-O chains, running along the *a* axis, shorten their interatomic distances along the chain. Consequently, the  $CuO_2$  layers are under compression along the a axis so that the  $CuO_4$  units in the  $CuO_2$  sheets become rectangular and the *a*-axis length becomes shorter than the *b*-axis length. How strongly the intralayer La-O, Tl-O, or Bi-O distances of the rock-salt layers can shorten is limited because of the  $CuO_2$  layer. The out-of-plane La- $O_{ax}$ , Tl- $O_{ax}$ , or Bi- $O_{ax}$  bond is not constrained by such restrictions and is therefore shortened considerably.

In the cuprate superconductors containing double rock-salt layers, the bonding between these two layers can be very different.<sup>13</sup> Between the double Bi–O layers of  $Bi_2Sr_2Ca_{n-1}Cu_nO_{2n+4}$ , there is only very weak inter-action because the  $Bi^{3+}$  6s lone-pair electrons are oriented between the sheets. A Bi-O chain in one of the sheets of the double layer is located directly above or below a chain in the other sheet of the double layer.<sup>10a</sup> This is in contrast to the staggered chain arrangements and very strong interlayer bonding found in the La-O layers of  $La_2CuO_4^{10a}$  and the Tl-O layers of (TlO)<sub>2</sub>-(BaO)<sub>2</sub>(Ca)<sub>n-1</sub>(CuO<sub>2</sub>)<sub>n</sub>.<sup>15</sup>

# Electronic Structure of the CuO<sub>2</sub> Layer

Oxidation formalism for cuprates is used to count the number of electrons in their d-block bands. In this counting scheme, the oxidation state of oxygen is assumed to be  $O^{2-}$ . Thus, a CuO<sub>2</sub> layer with formal copper oxidation state Cu<sup>2+</sup> has nine electrons to fill its d-block bands, so that its highest occupied band (i.e., the  $x^2 - y^2$  band) is half filled.<sup>16</sup> For a CuO<sub>2</sub> layer with formal copper oxidation state Cu<sup>(2+i)+</sup> ( $\epsilon > 0$ ), the  $x^2$  –  $y^2$  band is less than half filled (i.e.,  $1 - \epsilon$  electrons/  $CuO_2$ ). Cuprates with such  $CuO_2$  layers are p-type superconductors (with hole density  $n_{\rm H} = \epsilon/{\rm CuO}_2$  unit). For a  $CuO_2$  layer with formal copper oxidation state  $Cu^{(2-\epsilon)+}$ , the  $x^2 - y^2$  band is more than half filled (i.e.,  $1 + \epsilon$  electrons/CuO<sub>2</sub>). Cuprates with such CuO<sub>2</sub> layers are n-type superconductors (with electron density  $n_{\rm E} = \epsilon/{\rm CuO_2}$  unit).<sup>17</sup> The holes or electrons of the cuprate superconductors are probably all associated with the "in-plane"  $x^2 - y^2$  band, because this band lies signifi-

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(17) (a) Wang, E.; et al. Phys. Rev. B 1990, 41, 6582 and references therein. (b) The structure of the n-type cuprates can be described as an intergrowth between perovskite CuO<sub>2</sub> layers and fluorite-type rare-earth with the structure of the network. oxide layers.

cantly higher than the other d-block bands.

The electronic structures of cuprate superconductors are described by two widely different methods:<sup>18</sup> Α cluster approach (with Hubbard Hamiltonians) readily incorporates correlation energies and explains highenergy excitations (e.g., photoelectron spectra) well. However, the delocalized nature of the conduction electrons in the normal metallic state is not well described by this method. A band picture (with effective one-electron Hamiltonians) does not properly incorporate correlation energies and hence fails to explain details of high-energy excitation spectra and the insulating nature of those cuprates with only Cu<sup>2+</sup> ions in their  $CuO_2$  layers (e.g.,  $La_2CuO_4^{19}$  and  $YBa_2Cu_3O_6^{20}$ ). However, it is metallic cuprates that become superconductors when the temperature is lowered. The normal metallic states of these cuprates, in which the formal copper oxidation state differs from +2, are well described by a band picture because it accounts for the delocalized nature of the conduction electrons.<sup>18</sup> The insulating cuprates La<sub>2</sub>CuO<sub>4</sub> and YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6</sub> exhibit antiferromagnetism,<sup>19,20</sup> a special case of spin density wave (SDW), so that within a band picture the insulating nature of those cuprates with only  $Cu^{2+}$  ions in their  $CuO_2$  layers may be rationalized in terms of the metal-SDW transition<sup>21</sup> associated with the nested Fermi surfaces of their half-filled  $x^2 - y^2$  bands.<sup>22</sup> As the extent of hole- or electron-doping increases in the  $CuO_2$  layers, the Fermi surface becomes more circular in shape and therefore not nested so that the electronic instability resulting from the half-filled  $x^2 - y^2$  band is removed.

In the  $x^2 - y^2$  band of a layered cuprate, the copper  $x^2 - y^2$  orbitals make  $\sigma$  antibonding interactions with the oxygen orbitals. The extent of this antibonding increases gradually as the energy level is raised from the bottom to the top of the  $x^2 - y^2$  band. For instance, the bottom, middle, and top levels of this band are described by the orbitals 3a, 3b, and 3c, respectively.<sup>16,22</sup>



In fact, recent photoemission spectroscopy studies on cuprate superconductors reveal that the states around their Fermi levels have extensive copper d and oxygen p orbital hybridization.<sup>18b</sup> Due to the  $\delta$ -symmetry of the  $x^2 - y^2$  orbital along the Cu–O<sub>ax</sub> direction, the s and p orbitals of  $O_{ax}$  do not overlap with the  $x^2 - y^2$  orbitals of the CuO<sub>2</sub> layer copper atoms and therefore do not contribute to the  $x^2 - y^2$  band. Consequently, holedoping  $(n_{\rm H} > 0)$  or electron-doping  $(n_{\rm E} > 0)$  into the  $CuO_2$  layers affects electronically only the in-plane Cu-O bonds. The out-of-plane Cu-O bonds (i.e., Cu-

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O<sub>av</sub> bonds) are not electronically modified by hole- or electron-doping. That hole- or electron-doping in the cuprate systems involves only the  $\sigma$  antibonding inplane band (i.e., the  $x^2 - y^2$  band) of their CuO<sub>2</sub> layers has important geometrical consequences. Substitution of the larger cation La<sup>3+</sup> for the smaller cation Nd<sup>3+</sup> in  $Nd_{2-x}La_{x}CuO_{4}$  increases both the *a* and *c* unit cell parameters.<sup>17a</sup> This cation substitution does not alter the copper oxidation state, and the steric effect of the larger  $La^{3+}$  cation expands both the *a* and *c* parameters, which are associated with the in-plane and the out-of-plane Cu-O bond lengths, respectively. Substitution of the larger cation  $Sr^{2+}$  for the smaller cation  $La^{3+}$  in  $La_{2-x}Sr_{x}CuO_{4}$  increases the c parameter but decreases the a parameter.<sup>17a</sup> The latter is due to the electronic factor: substitution of  $Sr^{2+}$  for La<sup>3+</sup> creates holes in the  $CuO_2$  layer, i.e., removes electrons from the  $\sigma$  antibonding  $x^2 - y^2$  band. Likewise, substitution of the smaller cation Ce<sup>4+</sup> for the larger cation Nd<sup>3+</sup> in  $Nd_{2-x}Ce_{x}CuO_{4}$  decreases the c parameter but increases the a parameter,<sup>17a</sup> the latter being caused by the electronic factor of adding electrons in the antibonding  $x^2 - y^2$  band.

### **Rock-Salt Layer as Hole Source**

Hole-doping of the cuprate CuO<sub>2</sub> layers is achieved by several means, which include cation substitution, cation vacancy, and oxygen excess. All of these are based upon nonstoichiometry of chemical compositions. Holes may also be introduced into the  $CuO_2$  layers when the bottom of the rock-salt-layer bands lies below the Fermi level. This possibility becomes important for the cuprates containing Bi-O and Tl-O rock-salt layers because the 6p-block bands of the Bi-O layers and the 6s-block bands of the Tl-O layers lie close to the  $CuO_2$ -layer  $x^2 - y^2$  bands. According to band-structure calculations on  $Bi_2Sr_2Ca_{n-1}Cu_nO_{2n+4}$  with an ideal structure for the Bi-O double rock-salt layer, the bottom of the Bi 6p-block bands lies below the Fermi level.<sup>23</sup> This leads to a chemically unreasonable implication that Cu<sup>2+</sup> is oxidized by Bi<sup>3+</sup>. However, calculations with distorted Bi-O rock-salt-layer structures show<sup>24</sup> that the bottom of the Bi 6p-block bands of  $Bi_2Sr_2Ca_{n-1}Cu_nO_{2n+4}$  lies more than 1 eV above the Fermi level (see Figure 2a), and thus the Bi 6p-block bands do not act as a hole source. This finding is consistent with recent experimental observations.<sup>25</sup> Holes in  $Bi_2Sr_2Ca_{n-1}Cu_nO_{2n+4}$  are in part created by excess oxygen atoms in the Bi-O layers<sup>1b,24</sup> and in part by strontium deficiency.<sup>1b</sup> According to band-structure calculations<sup>26</sup> on  $Tl_2Ba_2Ca_{n-1}Cu_nO_{2n+4}$  with an ideal structure for the Tl-O double rock-salt layers, the bottom of their Tl 6s-block bands lies only slightly below the Fermi level, thereby suggesting that the Tl-O double rock-salt layer is not an important hole source. However, calculations with distorted Tl-O double rock-salt-layer structures reveal<sup>27</sup> that the bottom of the Tl 6s-block bands lies significantly below the Fermi level (see Figure 2b). Therefore, the Tl-O double

(26) For example, see: Yu, J.; Massidda, S.; Freeman, A. J. Physica C 1988, 152, 251.



Figure 2. Schematic representations for the relative energies of the CuO<sub>2</sub>-layer  $x^2 - y^2$  and the rock-salt-layer 6s- or 6p-block bands in (a)  $Bi_2Sr_2Ca_{n-1}Cu_nO_{2n+4}$ , (b)  $Tl_2Ba_2Ca_{n-1}Cu_nO_{2n+4}$ , (c)  $TlBa_2Ca_{n-1}Cu_nO_{2n+3}$ , and (d)  $Tl(SrR)CuO_5$  (R = La, Nd).

rock-salt layers are important in creating holes in the CuO<sub>2</sub> layers. Tl<sub>2</sub>Ba<sub>2</sub>CuO<sub>6</sub> exhibits<sup>13</sup> a  $T_c$  nearly as high as that of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> ( $T_c \approx 93$  K) although it has only one  $CuO_2$  layer/formula unit. This may reflect the fact that Tl<sub>2</sub>Ba<sub>2</sub>CuO<sub>6</sub> readily achieves a high copper oxidation state by the Tl 6s-block band/Cu  $x^2 - y^2$  band overlap plus additional hole sources such as excess oxygen and cation vacancy.

In sharp contrast to the case of the Tl-O double rock-salt-layer phases  $Tl_2Ba_2Ca_{n-1}Cu_nO_{2n+4}$ , however, band-structure calculations on the Tl-O single rocksalt-layer phases  $TlBa_2Ca_{n-1}Cu_nO_{2n+3}$  show<sup>27</sup> that the bottom of their Tl 6s-block bands lies well above the Fermi level (see Figure 2c). Therefore, the Tl-O single rock-salt layers of  $TlBa_2Ca_{n-1}Cu_nO_{2n+3}$  do not create holes in the  $CuO_2$  layers. This finding is consistent with the observation that stoichiometric  $TlBa_2Ca_{n-1}Cu_nO_{2n+3}$ already has copper atoms of high enough oxidation state [i.e., 2 + (1/n)], in contrast to stoichiometric doublephases  $Tl_2Ba_2Ca_{n-1}Cu_nO_{2n+4}$ layer and  $Bi_2Sr_2Ca_{n-1}Cu_nO_{2n+4}$  for which the copper oxidation state is +2. Tl-O single rock-salt layers are also found in the modified 1201-phase Tl(BaR)CuO<sub>5</sub> and Tl- $(SrR)CuO_5$  (R = La, Nd), in which the formal copper oxidation state is expected to be  $Cu^{2+}$ . Thus, it is hardly surprising that Tl(BaR)CuO<sub>5</sub> is not a superconductor.<sup>28</sup> Unexpectedly, however, Tl(SrR)CuO<sub>5</sub> is a superconductor.<sup>29</sup> This is due to its very short in-plane Cu-O bond.<sup>30</sup> Since the  $x^2 - y^2$  band is antibonding between the copper and in-plane oxygen atoms, shortening of the in-plane Cu-O bond raises the band in energy. This energy raising is high enough in  $Tl(SrR)CuO_5$  for the Fermi level to rise above the bottom of the Tl 6s-block bands (see Figure 2d),<sup>30</sup> so that the Tl–O single rock-salt layer creates holes in the  $CuO_2$  layer. The in-plane Cu-O bond is considerably shorter in  $Tl(SrR)CuO_5$  than in Tl(BaR)CuO<sub>5</sub> (i.e.,  $\sim$ 1.88 versus 1.93 Å)<sup>30</sup> because, on the average, smaller cations occupy the 9-coordinate sites in  $Tl(SrR)CuO_5$  (see below).

## T<sub>c</sub> versus In-Plane Cu-O Bond Length Correlation

Oxidation of the  $CuO_2$  layers removes electrons from the  $x^2 - y^2$  bands which have antibonding character in

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**Figure 3.** Correlation between the  $T_c$  and  $r_{Cu-O}$  values of various copper oxide superconductors.<sup>3</sup> The Ba, Sr and La classes are given by circles, triangles, and squares, respectively.

the in-plane Cu–O bonds. As  $n_{\rm H}$  increases, therefore, the in-plane Cu–O bond length  $(r_{Cu-O})$  is shortened. In addition to this electronic factor, the in-plane  $r_{Cu-O}$  is also controlled by the nonelectronic factor (for example, steric strain) associated with the cations located at the 9-coordinate sites adjacent to the  $CuO_2$  layers (see Figure 1).<sup>3</sup> With the increasing size of the 9-coordinate-site cations, the in-plane Cu-O bond is lengthened to reduce the extent of the resulting steric strain. Plots of  $T_{\rm c}$  versus in-plane  $r_{\rm Cu-O}$  (Figure 3) for the series of p-type cuprate superconductors are grouped into three classes distinguished by the size of the 9-coordinate-site cations (that is, La, Sr, and Ba classes) because of the combined electronic and nonelectronic effects.<sup>3</sup> The Sr and Ba classes contain subclasses which are further distinguished by a secondary nonelectronic factor associated with the number of CuO<sub>2</sub> layers/unit cell or the cation substitution in the rock-salt layers. Every class or subclass of the  $T_{\rm c}$  versus in-plane  $r_{\rm Cu-O}$  plot shows a maximum, so that every class or subclass of the p-type cuprate superconductors possesses an optimum hole density  $(n_{opt})$  for which the  $T_c$  is maximum

 $(T_{c,max})^3$ The  $T_{c,max}$  values of the three classes increase in the order La < Sr < Ba, and so do their corresponding in-plane  $r_{Cu-O}$  values  $(r_{opt})$ . Thus, for the p-type cuprates, a higher  $T_{c,max}$  results from a longer in-plane  $r_{Cu-O}$ . For the n-type cuprates as well, the  $T_c$  versus in-plane  $r_{Cu-O}$  plot exhibits a maximum.<sup>17a</sup> Compared with the Ba-class p-type cuprates, the n-type cuprates have a longer  $r_{opt}$  ( $\approx$ 1.975 Å) but a lower  $T_{c,max}$  (<30 K).<sup>17a</sup> Figure 4 shows the  $T_{c,max}$  versus  $r_{opt}$  plot based upon the three classes of the p-type cuprates and the n-type cuprates. This plot has a dome shape: The  $T_{c,max}$  increases with increasing the in-plane  $r_{Cu-O}$  when the latter is smaller than a critical value  $(r_c)$ , while the opposite is the case when  $r_{Cu-O} > r_c$ .

### Bond Valence Sum Analyses

The bond valence  $s_i$  of a bond *i* is defined as  $s_i = \exp[(r_0 - r_i)/0.37]$ <sup>31</sup> where  $r_i$  is the length of the bond *i*, and  $r_0$  is the constant that depends upon the atoms con-



Figure 4. Plot of  $T_{c,max}$  versus  $r_{opt}$  for the cuprate superconductors, where the solid line is a guide to the eye.



**Figure 5.**  $T_c$  versus in-plane copper BVS plot for the La-, Sr-, and Ba-class and -subclass superconductors. The symbols are defined as follows: O, Ba class;  $\Delta$ , Sr class;  $\Box$ , La class;  $\bullet$ ,  $(Tl_{2-x}Cd_x)Ba_2CuO_6$  subclass;  $\blacktriangle$ ,  $Bi_2Sr_2(Ca_{1-x}Y_x)Cu_2O_6$  subclass; +,  $(Tl_{0.5}Bi_{0.5})Sr_2(Ca_{1-x}Y_x)Cu_2O_7$  subclass. Each solid line represents the quadratic function of in-plane BVS obtained by least-squares fitting.

stituting the bond. For a metal atom surrounded by several identical ligands with bond lengths  $r_i$ , its bond valence sum (BVS) is given by the sum of all the bond valences  $\sum s_i$ . The BVS of the metal atom is a measure of the total amount of electrons it loses, that is, the formal oxidation state of the atom. The lengths of the chemical bonds in crystalline materials are determined by the electronic factor, which reflects the amounts of electrons in the bonds, and also by the nonelectronic factor which alters the bond lengths without changing the amounts of electrons in the bonds. As examples, we calculated the BVS values for the B cations of some perovskite phases,  $ABO_3$  (A = Ba, Sr; B = Ti), and  $K_2NiF_4$  structures,  $A_2BO_4$  (A = Ba, Sr; B = Sn). In these systems, the formal oxidation states of the A and B cations remain constant although their B-O bond length changes as a function of the A cation size. In other words, the B-O bond length change in these systems is solely governed by the steric factor associated with the A cation size: as the A cation size increases, the B-O bond length increases, thereby decreasing the BVS value of the B cation. The dependence of the BVS values upon the A cation size is substantial, so that BVS values cannot be used as a measure of formal oxidation states unless the steric factor is constant.<sup>2a</sup>

By definition, the bond valence of any given bond should increase with the shortening of its length. Because the in-plane  $r_{Cu-O}$  decreases with increasing  $n_{H}$ , the BVS of an in-plane Cu atom obtained only from its in-plane Cu-O bonds (referred to as the in-plane BVS)

<sup>(31)</sup> Brown, I. D.; Altermatt, D. Acta Crystallogr. B 1985, 41, 244.

should increase with increasing  $n_{\rm H}$ . Figure 5 shows how the  $T_{\rm c}$  values of the p-type cuprate superconductors are related to their in-plane BVS values for copper.<sup>2a</sup> Clearly these  $T_{\rm c}$  versus in-plane BVS plots are grouped into La, Sr, and Ba classes, and the Sr and Ba classes each contain subclasses, just as in the case of the  $T_c$  versus in-plane  $r_{Cu-O}$  correlation.<sup>3</sup> As shown by a solid line passing through each class or subclass, the  $T_{\rm c}$  values are well approximated by a quadratic function of inplane BVS, and each class or subclass shows a maximum. With the larger 9-coordination-site cation, the in-plane Cu–O bond is more stretched out so that the maximum of the corresponding  $T_{\rm c}$  versus in-plane BVS plot is shifted toward the direction of smaller BVS values. Within each class or subclass, the steric effect of the 9-coordinate-site cation is fairly constant so that a change in the in-plane BVS value becomes a reliable measure of the change in  $n_{\rm H}$ .<sup>2a</sup>

In YBa<sub>2</sub>Cu<sub>3</sub>O<sub>y</sub> (y = 7), the oxygen atoms of the Cu–O chains (that is, O<sub>ch</sub>) are gradually lost as y decreases from 7 to 6.<sup>32</sup> Aside from the Ba<sup>2+</sup> cations, the in-plane Cu–O bonds of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>y</sub> are also influenced by the steric effect of the O<sub>ch</sub> atoms, which lengthen the inplane Cu–O bonds parallel to the Cu–O chain direction.<sup>2a</sup> Thus, only the length variation of the in-plane Cu–O bonds perpendicular to the Cu–O chain direction is directly related to the hole density change in the CuO<sub>2</sub> layer. Use of only these in-plane Cu–O bonds in BVS analyses clearly demonstrates that the  $T_c$  versus y plot for YBa<sub>2</sub>Cu<sub>3</sub>O<sub>y</sub> reflects step-like increases in  $n_{\rm H}$  as y varies from 6 to 7.<sup>2a</sup>

### Toward Quantitative Structure-Property Relationships

Let us denote the in-plane BVS term by V and the optimum in-plane BVS corresponding to the  $T_{c,max}$  value by  $V_{opt}$ . As shown in Figure 5, the  $T_c$  and Vvalues of each class or subclass are well correlated with the expression  $\Delta T_c = -\alpha (\Delta V)^2$ , where  $\alpha$  is a positive constant,  $\Delta V = V - V_{opt}$ , and  $\Delta T_c = T_c - T_{c,max}$ .<sup>2a</sup> Within a class or subclass, the change  $\Delta V$  is proportional to the corresponding change in hole density, so that the  $T_{\rm c}$  and  $n_{\rm H}$  values for each class or subclass should be governed by the expression  $\Delta T_{\rm c} = -\beta (\Delta n_{\rm H})^2$ , where  $\beta$  is a positive constant, and  $\Delta n_{\rm H} = n_{\rm H} - n_{\rm opt}$ . In fact, the available experimental  $T_{\rm c}$  and  $n_{\rm H}$  values are well described by this expression, as shown in Figure 6.<sup>2a</sup> The  $\Delta T_c = -\alpha (\Delta V)^2$  and  $\Delta T_c = -\beta (\Delta n_H)^2$  expressions lead to the relationship  $\Delta n_H = (\alpha/\beta)^{1/2} \Delta V$ , which allows one to calculate the  $n_{\rm H}$  values from the observed in-plane Cu–O bond lengths. Figure 6 also shows the plots of  $T_c$  versus such calculated  $n_H$  values, referred to as  $n_H(BVS)$ . These plots are in essence identical with the corresponding experimentally determined  $T_{\rm c}$  versus  $n_{\rm H}$  plots.<sup>2a</sup> Because the  $\Delta T_{\rm c} = -\alpha (\Delta V)^2$  expression is good for all known p-type cuprate superconductors, the  $\Delta T_{\rm c} = -\beta (\Delta n_{\rm H})^2$  relationship should be valid for all known p-type cuprate superconductors, unless lattice instability sets in at a certain value of  $n_{\rm H}$  thereby giving rise to a structural phase transition as in the case of  $La_{2-x}Ba_xCuO_4$ .<sup>11</sup> The  $\Delta T_c = -\beta(\Delta n_H)^2$  expression is rewritten as<sup>2a</sup>



**Figure 6.** Comparison of the  $T_c$  versus  $n_H$  correlations  $(\Delta, \Box)$  with the  $T_c$  versus  $n_H(BVS)$  correlations  $(\Delta, \blacksquare)$ . The symbols are defined as follows:  $\Delta, \Delta$ ,  $Bi_2Sr_2(Ca_{1-x}Y_x)Cu_2O_8$  subclass;  $\Box, \blacksquare, La$  class. Each solid line represents the quadratic function of  $n_H$  or the  $n_H(BVS)$  obtained by least-squares fitting.

under the condition that  $|\Delta n_{\rm H}| \ll (1/\eta)^{1/2}$ , where  $\eta = \beta/T_{\rm c,max}$ . Equation 1 is found to be valid for most  $n_{\rm H}$  values around  $n_{\rm opt}$ .<sup>2a</sup>

For pairing due to exchange of phonons, spin fluctuations, or combined charge fluctuations and lattice distortions, the  $T_c$  and the coupling constant  $\lambda$  are governed by the expression<sup>33</sup>

$$T_{\rm c} \simeq \omega \exp\left[-(1+\lambda)/(\lambda-\delta)\right]$$
 (2)

where  $\omega$  is the average energy of the fluctuations of the pairing field and  $\delta$  is a small correction term. Equation 1 is formally equivalent to eq 2 so that, if the term  $\delta$ of eq 2 is neglected, eqs 1 and 2 give rise to the expression<sup>2a</sup>  $\lambda = \lambda_H + \lambda_0$ , where  $\lambda_0$  is independent of  $n_H$ and  $\lambda_H$  depends upon  $n_H$  as  $\lambda_H \propto n_H(C - n_H)$  (C is a positive constant). The magnitude of  $\lambda_H$  is governed by two opposing factors: one factor increases  $\lambda_H$  linearly with increasing  $n_H$  [i.e.,  $\lambda_H \propto n_H$ ] whereas the other factor decreases  $\lambda_H$  linearly with increasing  $n_H$  [i.e.,  $\lambda_H \propto (C - n_H)$ ]. Thus, the  $\lambda_H$  versus  $n_H$  plot has the shape of an inverted parabola as does the  $T_c$  versus  $n_H$  plot. It is crucial to understand the exact origin of the  $\lambda_H \propto n_H(C - n_H)$  relationship.

Ultimately, the physical properties of the cuprate superconductors should be describable on the basis of a proper model Hamiltonian which consists of phenomenological parameters such as the hopping (i.e., resonance) integral t, the on-site repulsion U, the intersite repulsion V, the bond-charge repulsion<sup>34</sup> B, etc. The  $T_{c,max}$  versus  $r_{opt}$  plot of Figure 4 shows that the  $r_{opt}$ values of the p-type cuprate classes increase in the order La < Sr < Ba class. Lengthening of the in-plane Cu–O bond decreases the magnitudes of the t, V, and B parameters associated with the copper  $x^2 - y^2$  and the oxygen p orbitals. Therefore, Figure 4 shows that, as the magnitudes of these parameters decrease, the  $T_{\rm c.max}$ value of the p-type cuprates increases whereas that of the n-type cuprates decreases. Any model Hamiltonian appropriate for the cuprate superconductors must reproduce these findings.<sup>35</sup>

It is important to note that the  $T_c$  and in-plane  $r_{Cu-O}$  values of the p- or n-type cuprates can be varied in a

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systematic manner without changing their  $n_{\rm H}$  or  $n_{\rm E}$ values. Examples include  $La_{1.85-x}Nd_xSr_{0.15}CuO_4^{36}$  and

 $Tl_2Ba_{2-x}Sr_xCaCu_2O_8^{37}$  in the p-type cuprates and  $Nd_{1.85-x}La_xCe_{0.15}CuO_4^{17a}$  in the n-type cuprates. Substitution of the 8- or 9-coordinate-site cations with isovalent cations of different size changes the in-plane  $r_{Cu-O}$  value, which modifies the magnitudes of the t, V, and B parameters, thereby changing the  $T_{\rm c}$ .

#### **Concluding Remarks**

In understanding the superconductivity of the cuprates, it is important to distinguish between steric and electronic factors. The  $T_c$  versus in-plane  $r_{Cu-O}$  and  $T_c$ versus in-plane BVS plots of the p-type cuprates are

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grouped into classes and subclasses due to steric factors. Electronic factors acting on each class or subclass are remarkably similar: the  $T_c$  is an inverted parabolic function of  $n_{\rm H}$ . This correlation suggests that the coupling constant for Cooper pair formation is also an inverted parabolic function of  $n_{\rm H}$ . Our study shows that, as the magnitudes of the t, V, and B parameters decrease, the  $T_{c,max}$  value of the p-type cuprates should increase whereas that of the n-type cuprates should decrease. These findings must be reproduced by any model Hamiltonian appropriate for the cuprate superconductors.

Work at North Carolina State University is supported by the Office of Basic Energy Sciences, Division of Materials Sciences, U.S. Department of Energy, under Grant DE-FG05-86ER45259. We thank Dr. B. H. Brandow for invaluable discussions.

# **Nonlinear Optical Properties of Nanometer-Sized Semiconductor Clusters**

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The field of nonlinear optics was launched almost 30 years ago by the observation of second harmonic generation in a quartz crystal.<sup>1</sup> Through intensive research in the following decades, the basic physics behind various nonlinear optical phenomena is now mostly understood.<sup>2</sup> With the maturity of the field, the focus has shifted to the study of nonlinear optical properties of materials, a subject receiving growing interest in recent years.<sup>3-5</sup> The primary objective is to find materials with exceptional nonlinear optical response for possible applications as optical switching and frequency conversion elements in the telecommunication and information processing industries. With this new emphasis and the exciting prospects of replacing electrons with photons in future photonic devices, a growing number of chemists and materials scientists have been attracted to the field. The study of optically nonlinear materials has evolved into a truly multidisciplinary area.

Materials under investigation are traditionally divided into three categories: organics,<sup>3</sup> inorganics,<sup>4</sup> and semiconductors.<sup>5</sup> Each of these classes of materials has its own merits and limitations and is suited for different types of applications. In this Account, I focus on a new class of materials, namely, nanometer-sized semiconductor clusters (sometimes called nanocrystallites, quantum dots, Q-particles, ..., etc.). These clusters possess structures that are essentially the same as bulk semiconductors, yet with properties dramatically different from those of the bulk; often they are better viewed as very large molecules.<sup>6-8</sup> The electronic properties of these clusters depend on the cluster size, a phenomenon commonly referred to as the quantum size or quantum confinement effect.<sup>6-12</sup> The effect is manifested as a blue shift in the exciton (an electronhole pair bounded by Coulomb interaction) energy and enhancement in the volume-normalized oscillator strength as the cluster size decreases. Several review papers<sup>6-8</sup> summarize the current status of the material synthesis and our understanding of their size-dependent electronic and photochemical properties.

Our studies of the nonlinear optical properties of these clusters were triggered by a paper<sup>13</sup> describing the nonlinear optical properties of commercial color filters (sold by both Corning and Schott). These color filters contain nominally  $CdS_xSe_{1-x}$  particles of ~100-1000-Å diameter,<sup>13</sup> a size regime where their optical properties still resemble those of the bulk. The reported large

<sup>†</sup>Contribution No. 5732.

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